

UNIVERSITY OF NORTH CAROLINA AT CHARLOTTE

Department of Electrical Engineering

Experiment No. _____ Balanced Three-Phase Networks

INTRODUCTION

Three-phase networks can be connected either in a "Delta" configuration such as in Figure 2 or a "Wye" configuration such as in Figure 4. For balanced loads, $Z_1 = Z_2 = Z_3$. Also, for a balanced delta-connection and an ABC sequence,

$$V\text{-phase} = V\text{-line} \quad (V_{AB}, V_{BC}, V_{CA})$$

$$I\text{-phase} = V\text{-phase}/Z\text{-phase} \quad (I_{AB}, I_{BC}, I_{CA})$$

$$I\text{-line} = I\text{-phase} \quad (I_A, I_B, I_C)$$

The line (phase) voltages are 120 electrical degrees apart. So are the line currents and the phase currents. A typical phasor diagram for a delta-connection is shown in Figure 3.

For a balanced wye-connection and an ABC sequence,

$$V\text{-phase} = (V\text{-line}/\sqrt{3}) \angle -30 \text{ degrees} \quad (V_{AN}, V_{BN}, V_{CN})$$

$$I\text{-phase} = V\text{-phase}/Z\text{-phase} \quad (I_{AN}, I_{BN}, I_{CN})$$

$$I\text{-line} = I\text{-phase} \quad (I_A, I_B, I_C)$$

Again, the line (phase) currents are 120 electrical degrees apart as are the line voltages and the phase voltages. A typical phasor diagram for a wye-connection is shown in Figure 5.

Total power for either connection would be,

$$S = 3 V\text{-phase} I^*\text{-phase} = P + jQ = \sqrt{P^2 + Q^2} \angle \text{atan} \frac{Q}{P}$$

$$|S| = \sqrt{3} |V\text{-line}| |I\text{-line}|$$

$$P = 3 |V\text{-phase}| |I\text{-phase}| \cos \angle V_p \& I_p = |S| \cos \angle V_p \& I_p$$

$$Q = 3 |V\text{-phase}| |I\text{-phase}| \sin \angle V_p \& I_p = |S| \sin \angle V_p \& I_p$$

$$P = 3 I^2 \text{-phase R-phase}$$

$$Q = 3 I^2 \text{-phase X-phase}$$

PRELIMINARY

P-1. Show mathematically and graphically that, $I_A + I_B + I_C = 0$, for a balanced three-phase network.

P-2. Prove mathematically that the two wattmeters in Figure 1 measures the total real power, P , for a balanced three-phase network.

(INSTRUCTOR'S SIGNATURE _____ DATE _____)

Suggested Reference

Electrical Engineering Circuits (2nd edition)
Hugh Hildreth Skilling
Chapter 20 - Three Phase Circuits

PROCEDURE

F-1. Connect one of the circuits below AFTER checking with the Instructor

Network No.	Connection	Impedance ($\omega = 377$)
1	Delta	$2000 + RL + j10\omega$
2	Wye	$2000 + RL + j10\omega$
3	Delta	$8000 + RL + j10\omega$
4	Wye	$8000 + RL + j10\omega$
5	Wye	$1000 - j1/(2 \times 10^{-6}\omega)$
6	Wye	$3000 - j1/(2 \times 10^{-6}\omega)$
7	Delta	$1000 - j1/(10^{-6}\omega)$
8	Wye	$1000 - j1/(10^{-6}\omega)$
9	Wye	$3000 - j1/(10^{-6}\omega)$

RL - the resistance of the inductor
 ω - frequency in radians/seconds

CAUTION: DO NOT MAKE CHANGES IN THE NETWORK UNLESS THE CIRCUITBREAKER IS OPEN!

The two wattmeters (Power Analyzers) should be connected as shown.

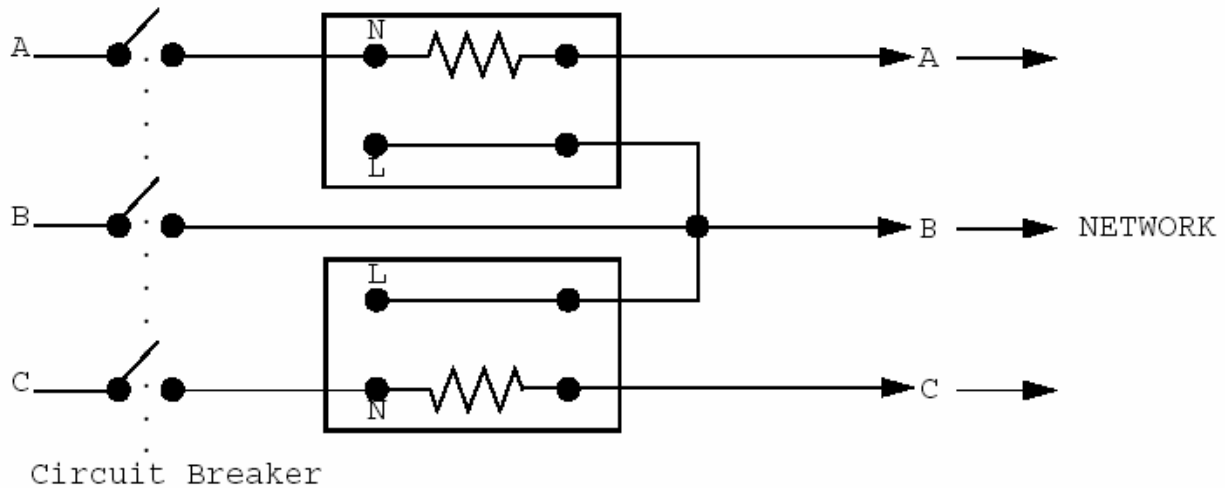


Figure 1.

F-2. Record the two power readings (with sign), the two line voltage readings, and the two line current readings.

F-3. Insert one of the wattmeters (Power Analyzer) into one of the phases. Record the phase voltage, phase current, and phase power readings.

REPORT

R-1. Using data from F-3, verify the per-phase load.

R-2. Calculate the phase voltage, phase current, line current, and total power (S , P , and Q) for the network tested using the given, measured line voltage and the theoretical given load.

R-3. In a table, compare S , P , Q , V -phase, I -phase, V -line, and I -line using the calculations in R-2, the data in F-2, and the data in F-3. Use the load found in R-1 to find S and Q from the data. Be sure the powers are total three-phase powers. Discuss any differences.

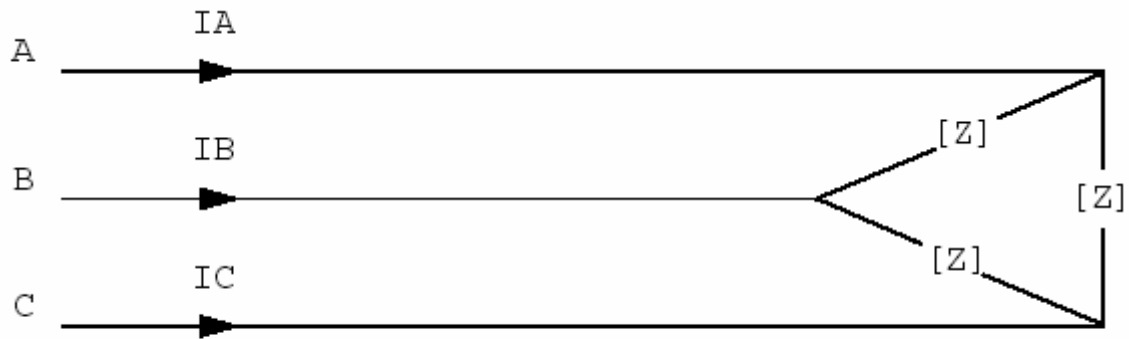


Figure 2.

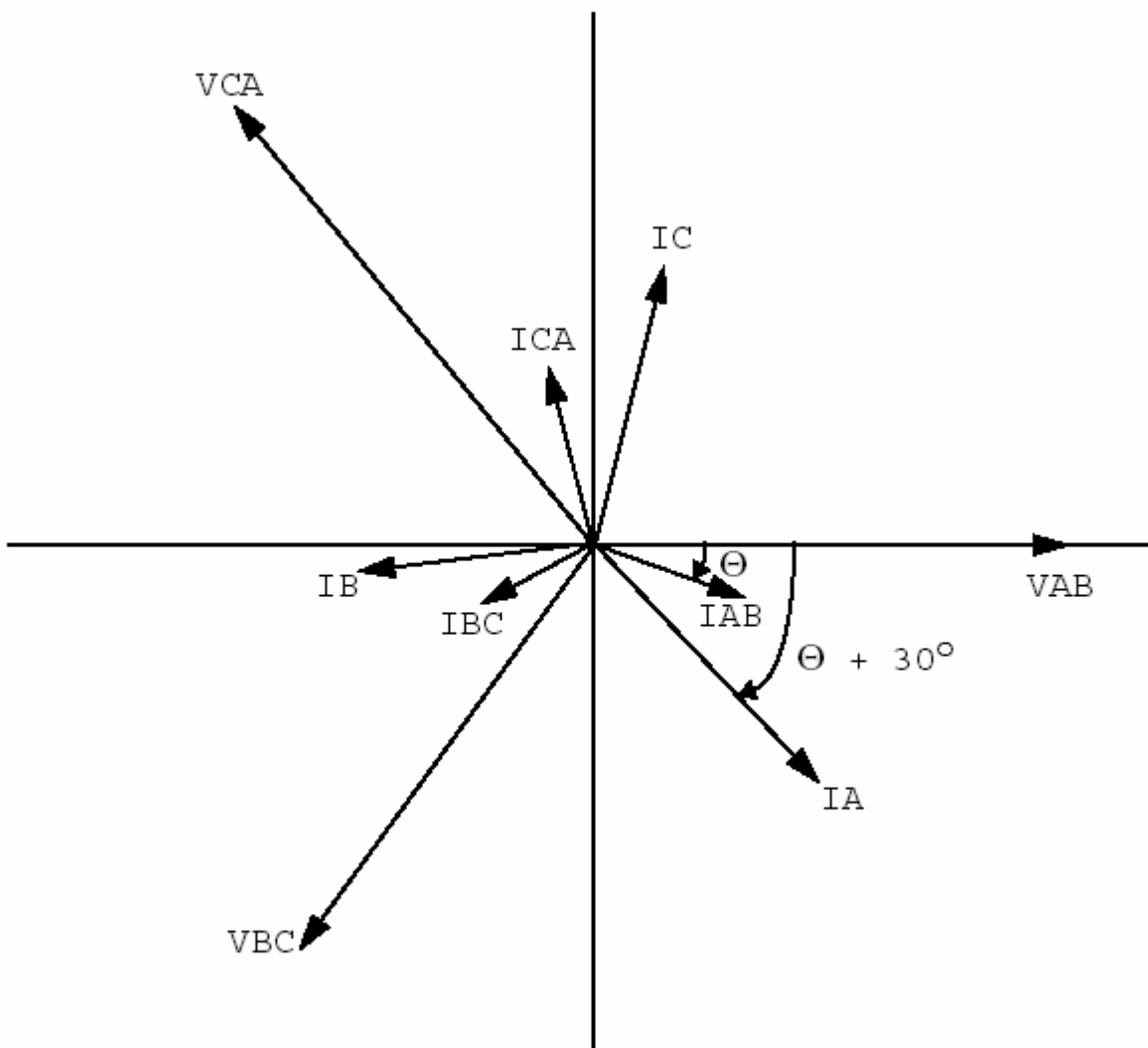


Figure 3.

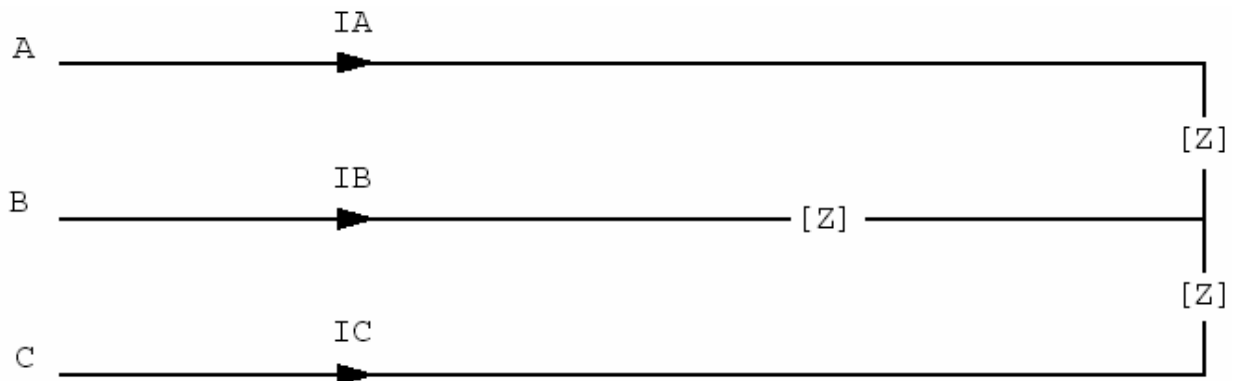


Figure 4.

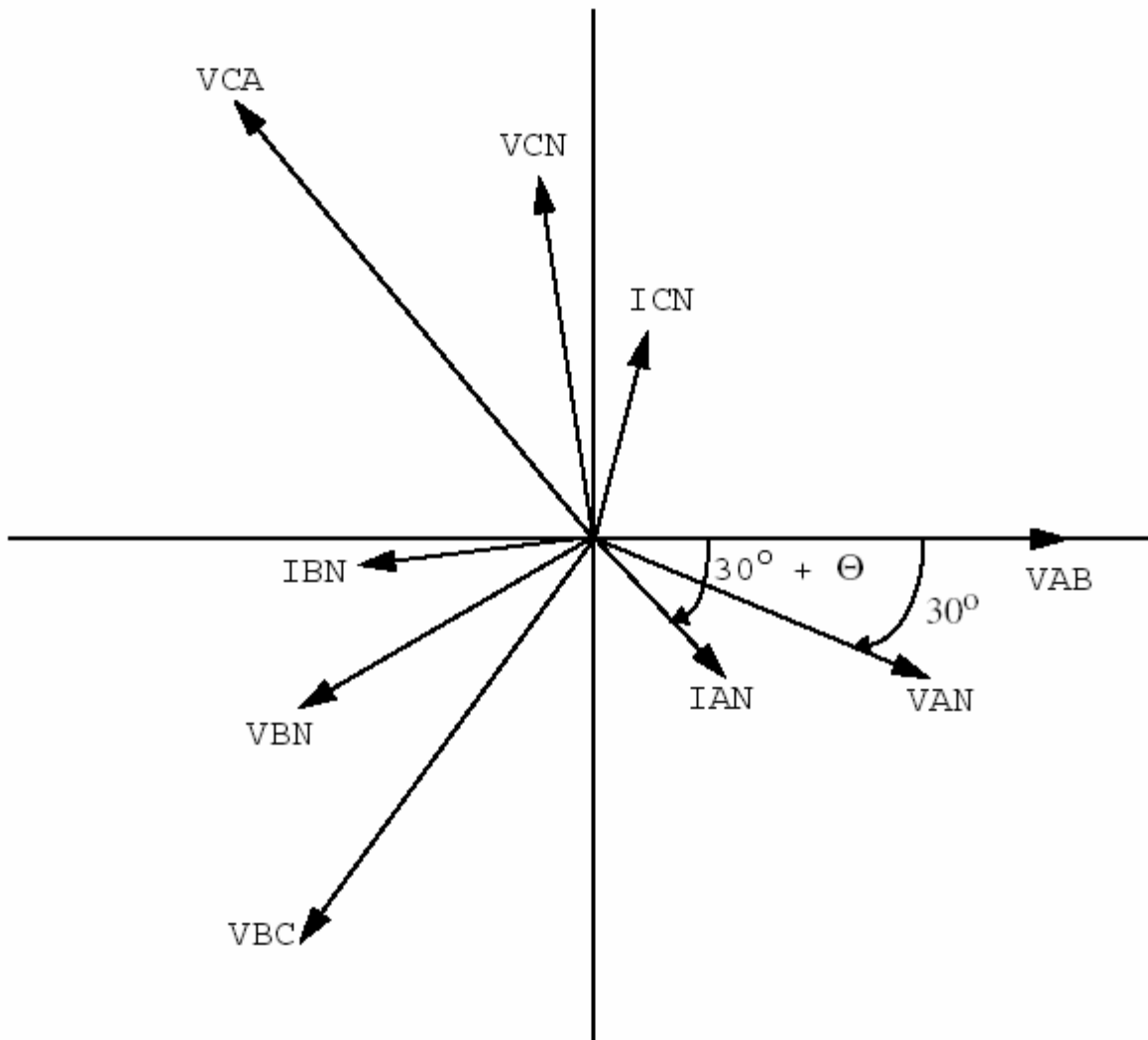


Figure 5.